

# Yambo à la carte



# Yambo



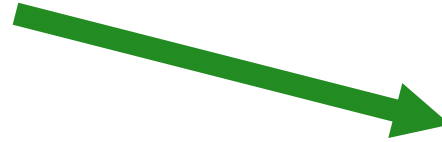
Yet Another Many  
Body code

Claudio Attaccalite

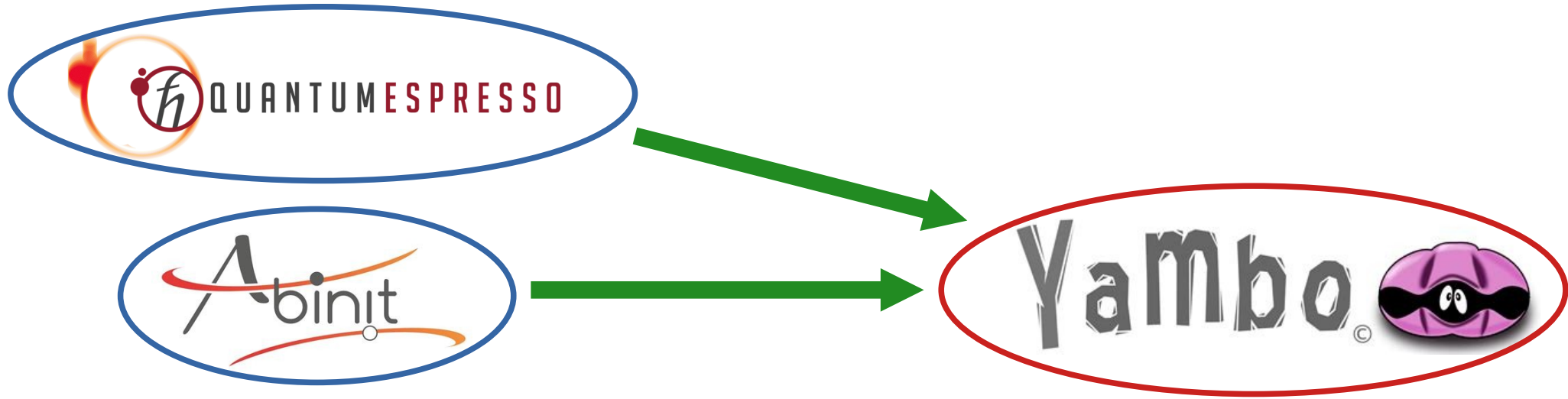


**Yambo** is a many-body code  
in a Kohn-Sham basis

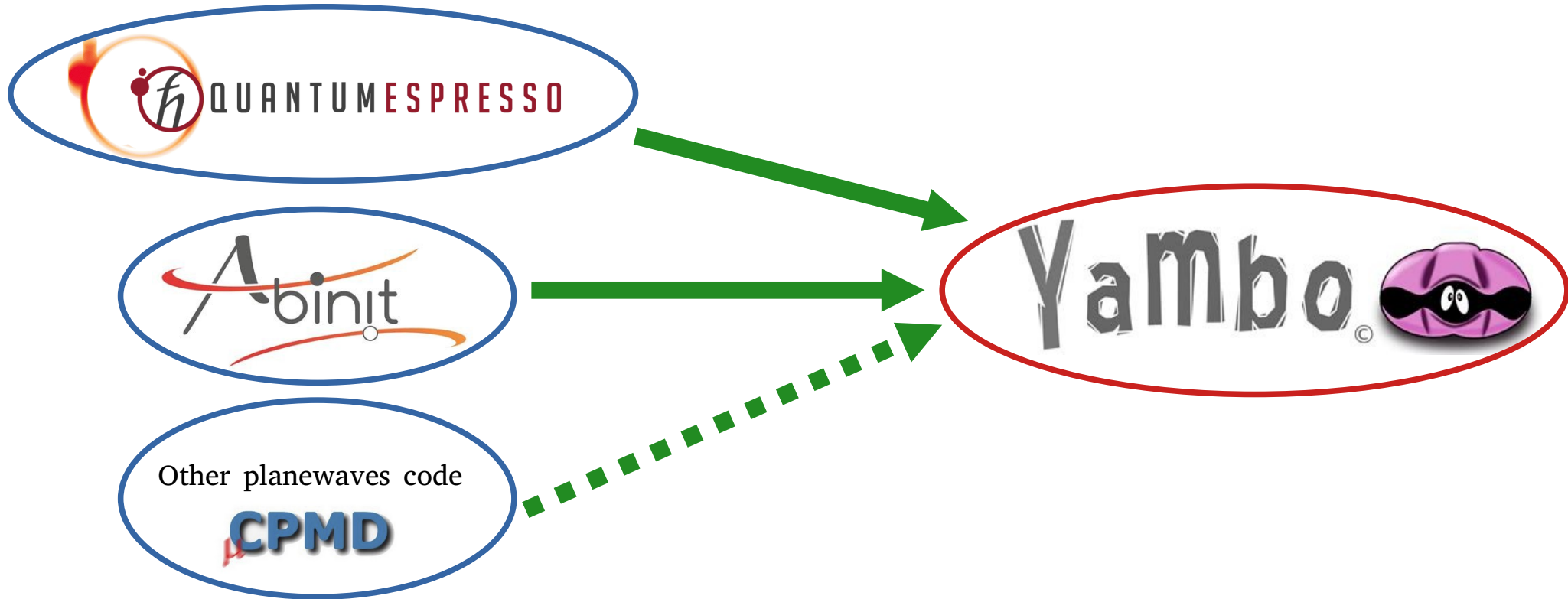
Yambo is a many-body code  
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# Yambo is a many-body code in a Kohn-Sham basis



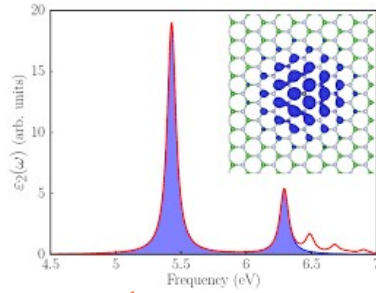
# Yambo is a many-body code in a Kohn-Sham basis



What can you do with **Yambo**?

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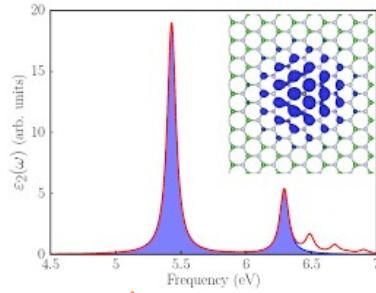
Optical properties



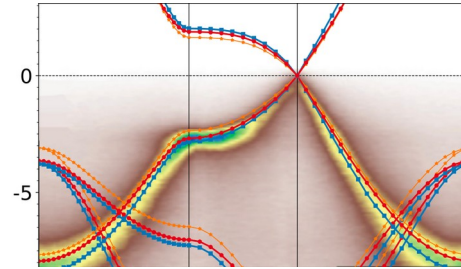


# What can you do with **Yambo**?

## Optical properties

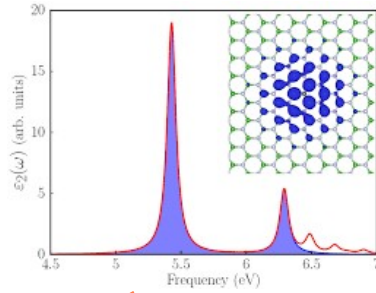


## Quasi-particle band structure

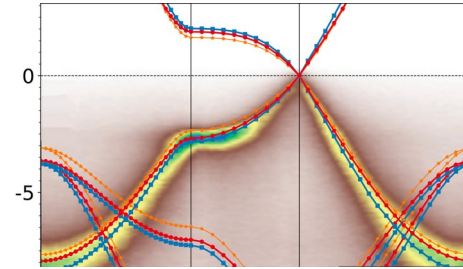


# What can you do with **Yambo**?

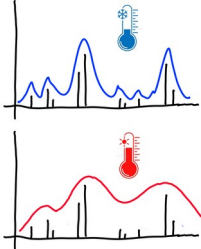
## Optical properties



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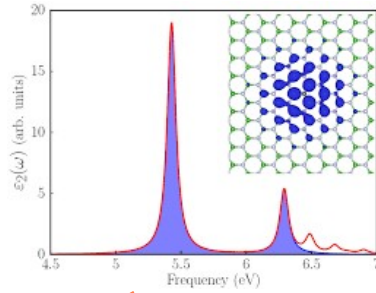


## Electron-phonon coupling

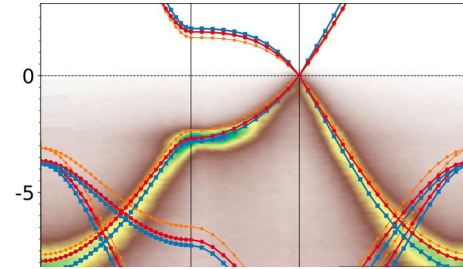


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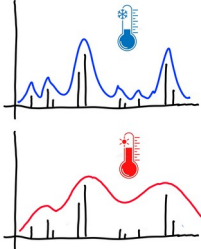
## Optical properties



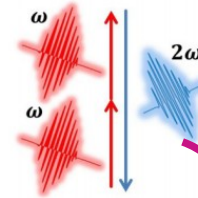
## Quasi-particle band structure



## Electron-phonon coupling

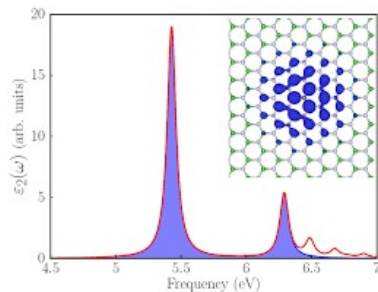


## Nonlinear optics

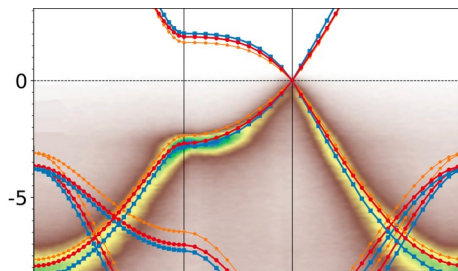


# What can you do with **Yambo**?

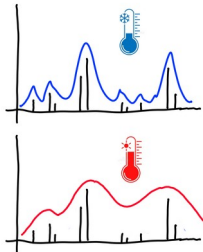
## Optical properties



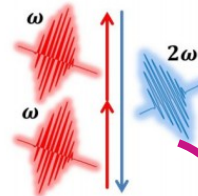
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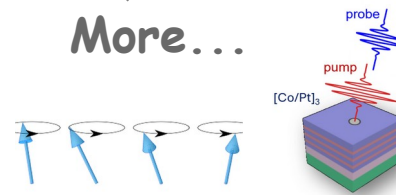
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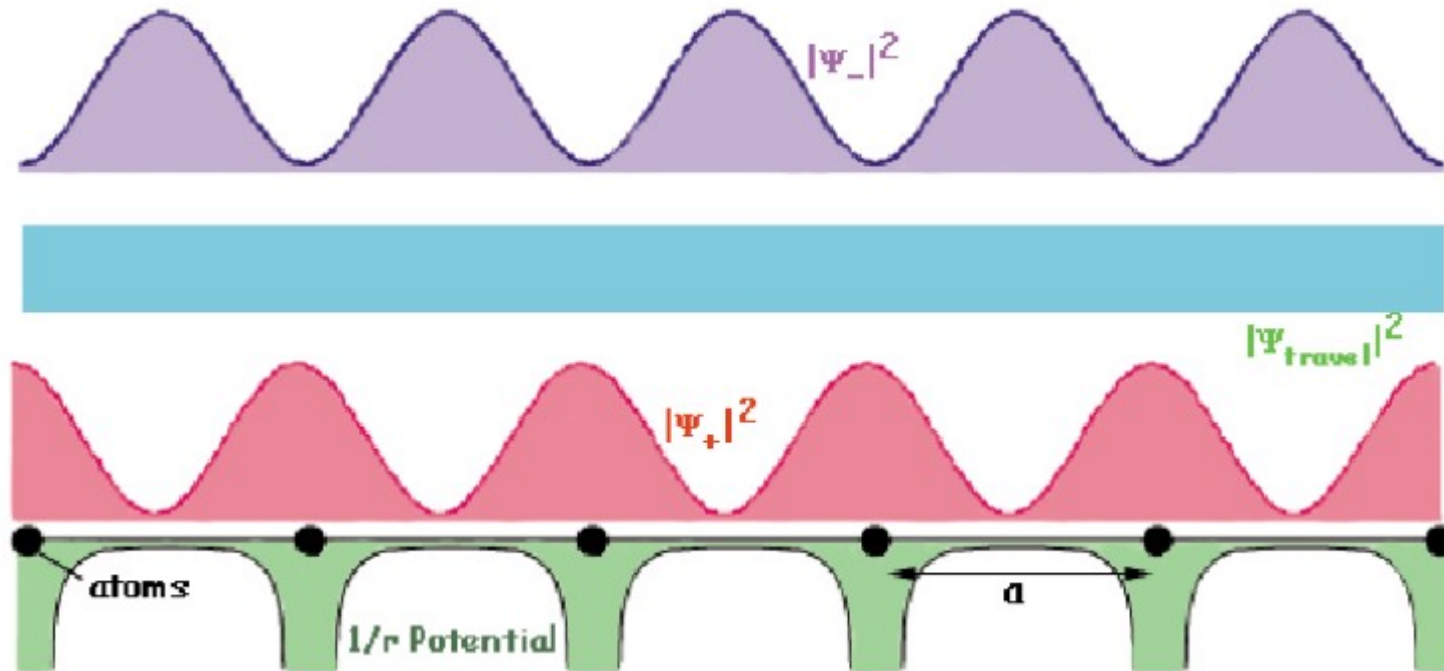
## Nonlinear optics



## More...



# Basis set



# The basis: KS and plane-waves 1/2

KS Bloch functions

$$|\phi_{n\mathbf{k}}\rangle = e^{i\mathbf{k}r} |u_{n\mathbf{k}}(r)\rangle$$

$$\langle u_{n\mathbf{k}}(r) | u_{m\mathbf{k}}(r) \rangle = \delta_{n,m}$$

KS basis set

# The basis: KS and plane-waves 1/2

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## KS basis set

$$H_{nm}(\mathbf{k}) = \langle u_{n\mathbf{k}} | \hat{H}(\mathbf{k}) | u_{m\mathbf{k}} \rangle$$

# The basis: KS and plane-waves 1/2

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## KS basis set

$$H_{nm}(\mathbf{k}) = \langle u_{n\mathbf{k}} | \hat{H}(\mathbf{k}) | u_{m\mathbf{k}} \rangle$$

$$A_{nm}(\mathbf{k}, \mathbf{k} + \mathbf{q}) = \langle u_{n\mathbf{k}} | \hat{A} | u_{m\mathbf{k}+\mathbf{q}} \rangle$$

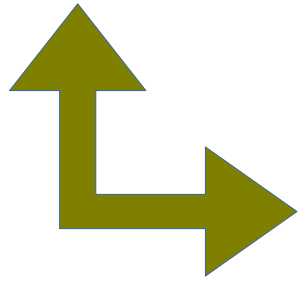


# The basis: KS and plane-waves 1/2

## KS Bloch functions

$$|\phi_{n\mathbf{k}}\rangle = e^{i\mathbf{k}r} |u_{n\mathbf{k}}(r)\rangle$$

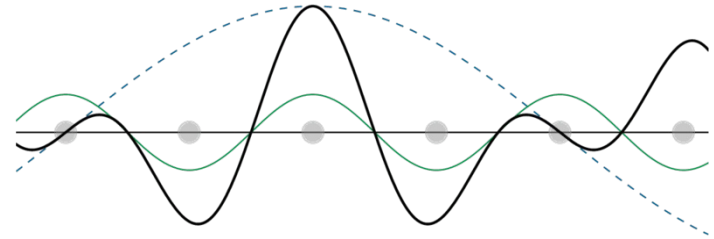
$$\langle u_{n\mathbf{k}}(r) | u_{m\mathbf{k}}(r) \rangle = \delta_{n,m}$$


$$|u_{n\mathbf{k}}\rangle = \sum_{\mathbf{G}} C_{\mathbf{G}}^{n\mathbf{k}} e^{i\mathbf{G}r}$$

## KS basis set

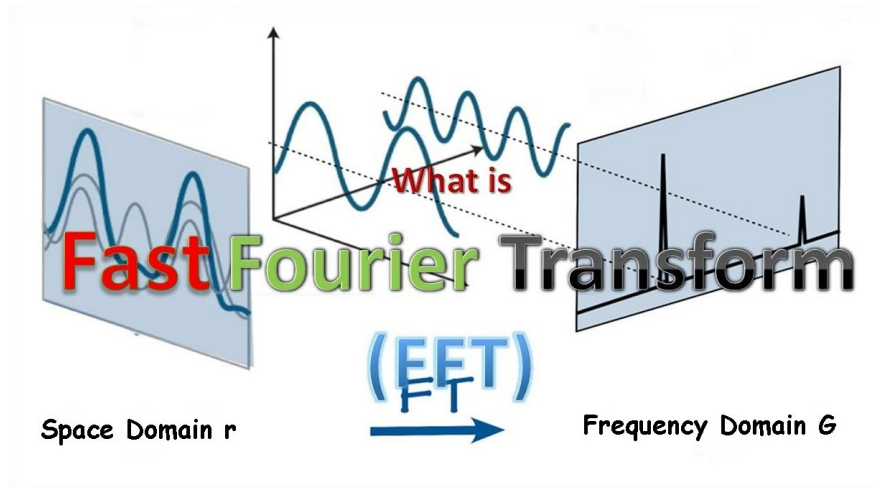
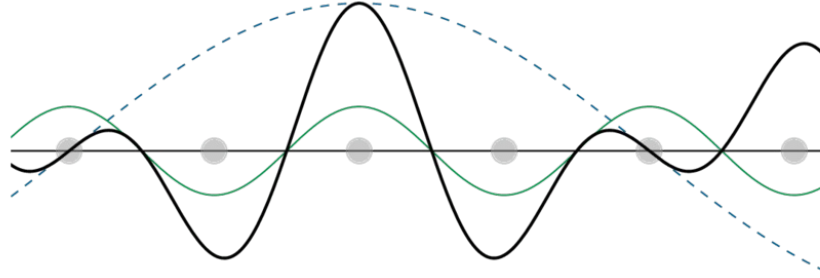
$$H_{nm}(\mathbf{k}) = \langle u_{n\mathbf{k}} | \hat{H}(\mathbf{k}) | u_{m\mathbf{k}} \rangle$$

$$A_{nm}(\mathbf{k}, \mathbf{k} + \mathbf{q}) = \langle u_{n\mathbf{k}} | \hat{A} | u_{m\mathbf{k}+\mathbf{q}} \rangle$$



# The basis: KS and plane-waves 2/2

$$|u_{n\mathbf{k}}\rangle = \sum_{\mathbf{G}} C_{\mathbf{G}}^{n\mathbf{k}} e^{i\mathbf{G}r}$$



$$\langle A \rangle_{n,m} = \langle u_{n\mathbf{k}}(r) | \hat{A}(r) | u_{n\mathbf{k}}(r) \rangle$$

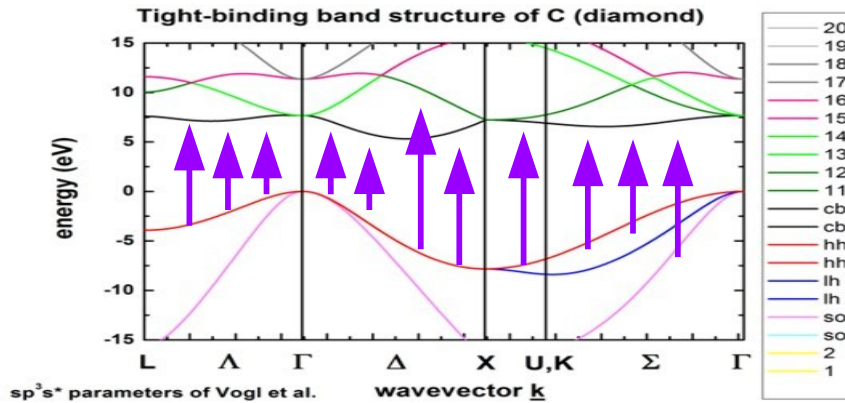
$$\langle B \rangle_{n,m} = \langle u_{n\mathbf{k}}(G) | \hat{B}(G) | u_{n\mathbf{k}}(G) \rangle$$

# Properties

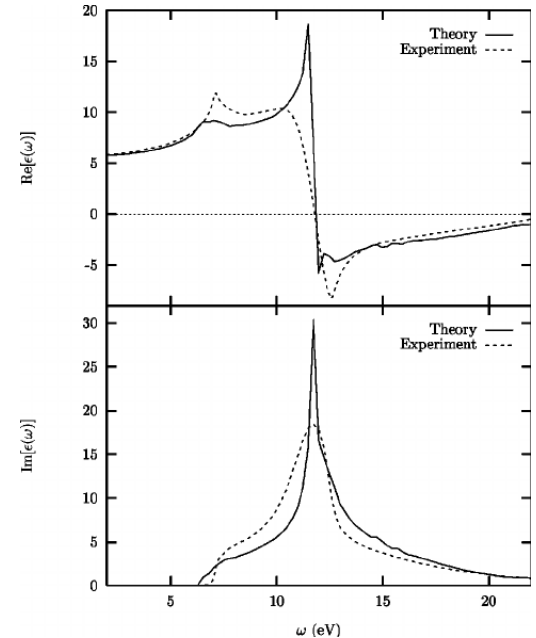


# Linear optical response

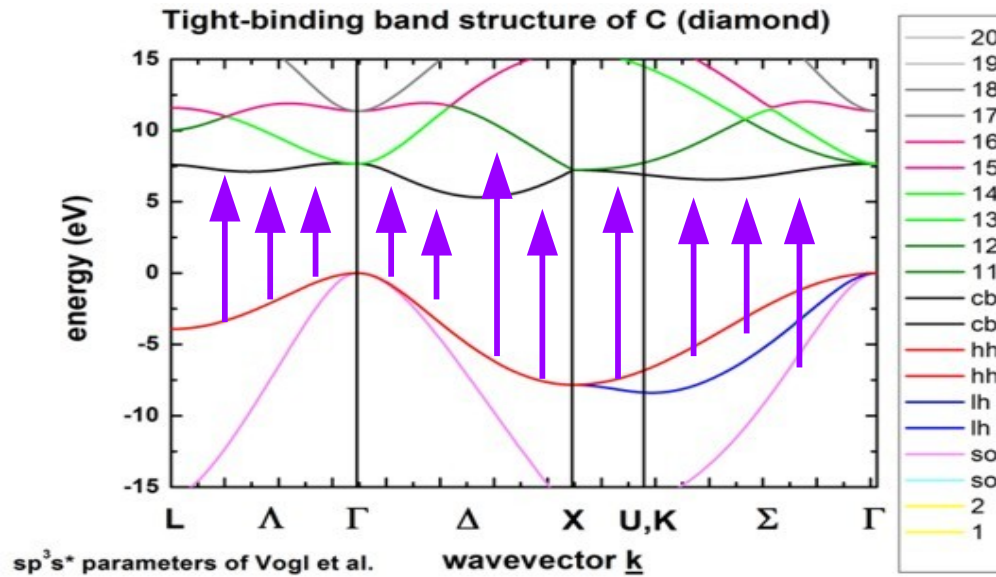
$$\epsilon(\omega) = 1 - \frac{4\pi}{V} \sum_{\mathbf{k}, v, c} \frac{|\langle \phi_{\mathbf{k}, v} | r | \phi_{\mathbf{k}, c} \rangle|^2}{\epsilon_{\mathbf{k}, v} - \epsilon_{\mathbf{k}, c} - \omega + i\eta}$$



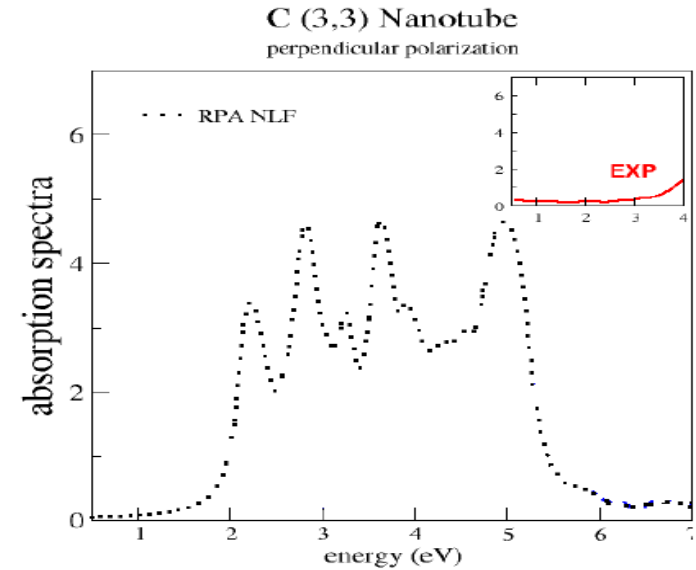
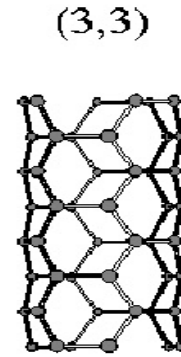
Electrons are excited from valence to conduction bands



# Local field effects 1/2

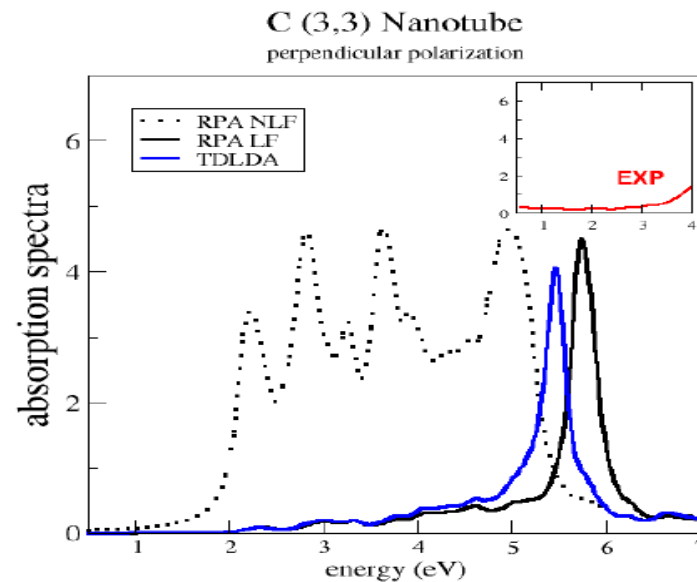
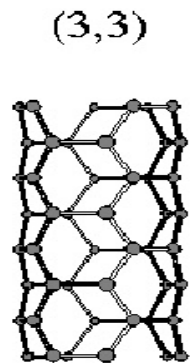
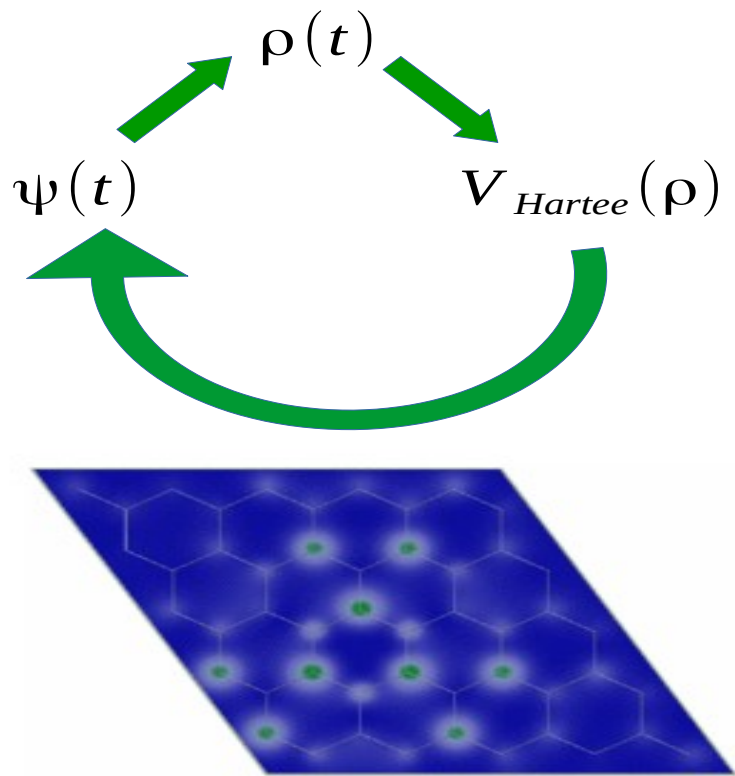


Electrons are excited from valence to conduction bands



Unfortunately these excitations are not independent

# Local field effects 2/2



$$\chi_{g,g'} = \chi^0 + \chi^0 V \chi$$

# TDDFT

... in  $g$ -space...

$$\chi = \chi^0 + \chi^0(V + f_{xc})\chi$$

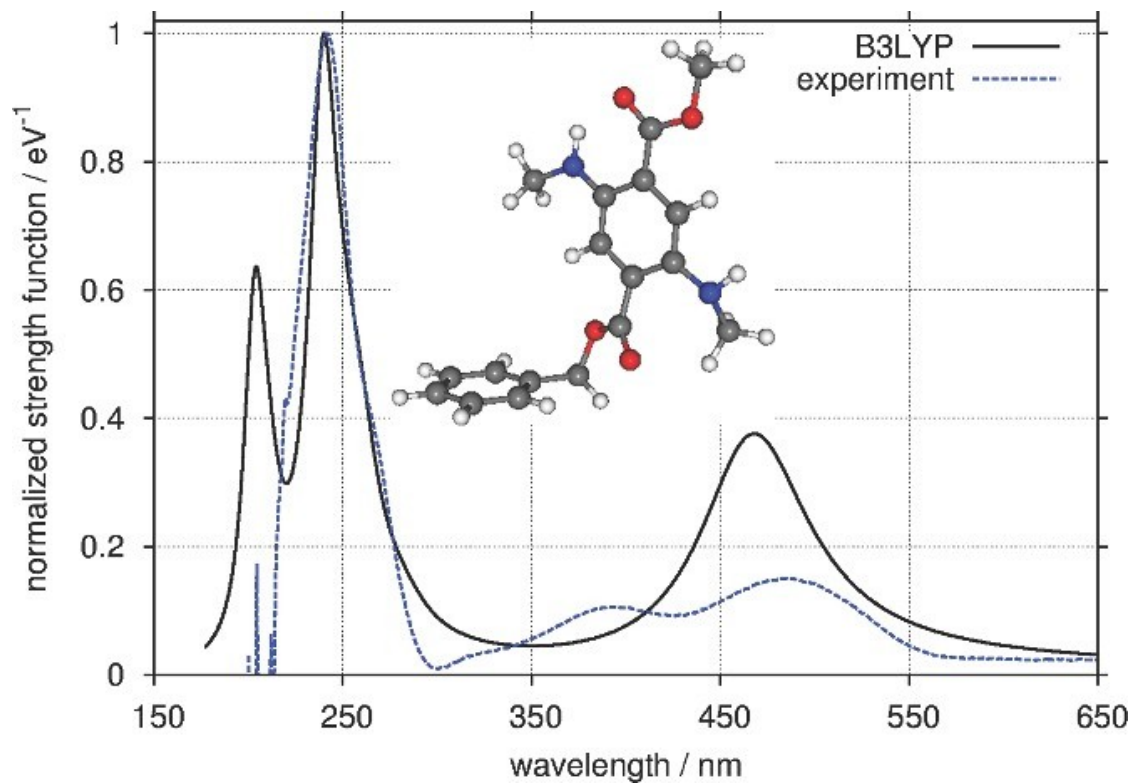
...or in e-h space (Casida eq.)...

$$\begin{bmatrix} A & B \\ B^* & A^* \end{bmatrix} \begin{bmatrix} X \\ Y \end{bmatrix} = \omega \begin{bmatrix} 1 & 0 \\ 0 & -1 \end{bmatrix} \begin{bmatrix} X \\ Y \end{bmatrix}$$

Tamm – Dancoff Approximation reduces equations to  $AX = \omega X$

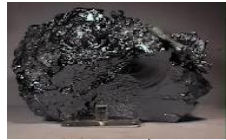
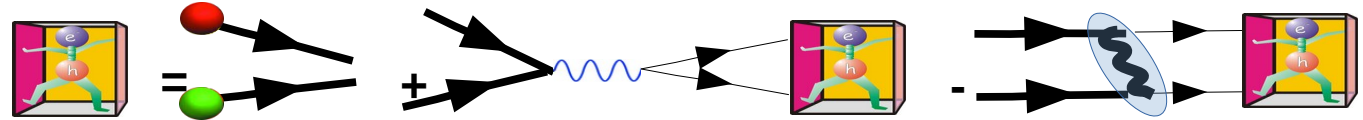
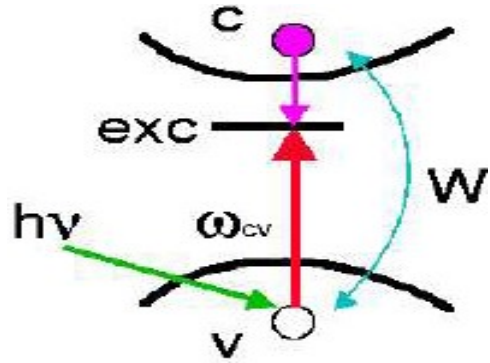
$$A = \delta_{ij}\delta_{ab}(\epsilon_a - \epsilon_i) + K_{ia,jb}$$

$$K_{ia,jb} = (pq|\frac{1}{r_{12}}|rs) + (pq|f_{xc}|rs)$$

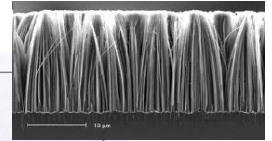
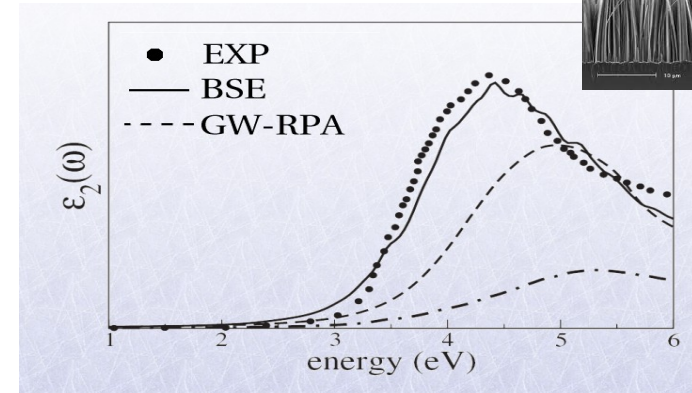
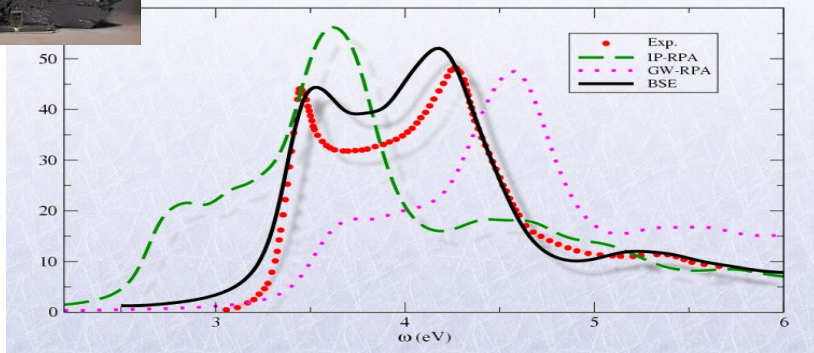




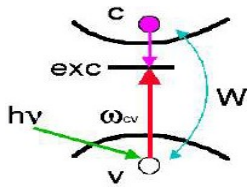
# Excitons



Absorption Spectrum of Silicon  
IP-RPA vs GW-RPA vs BSE vs exp.





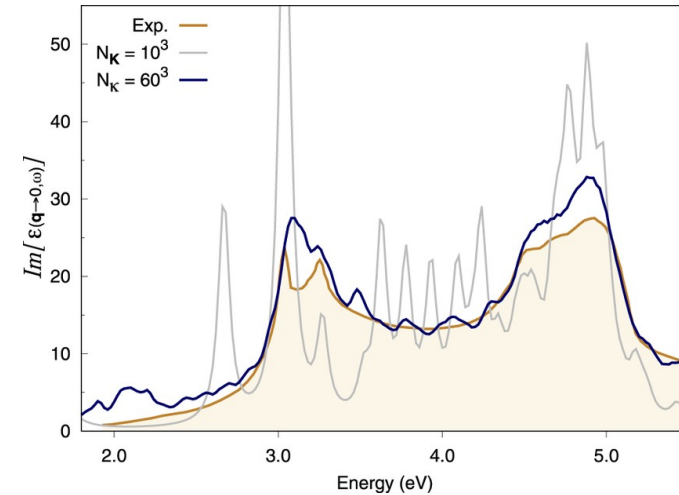
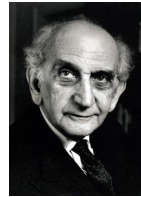
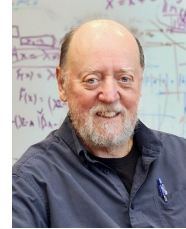
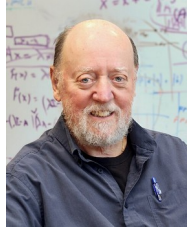


# Solving the Bethe-Salpeter equation

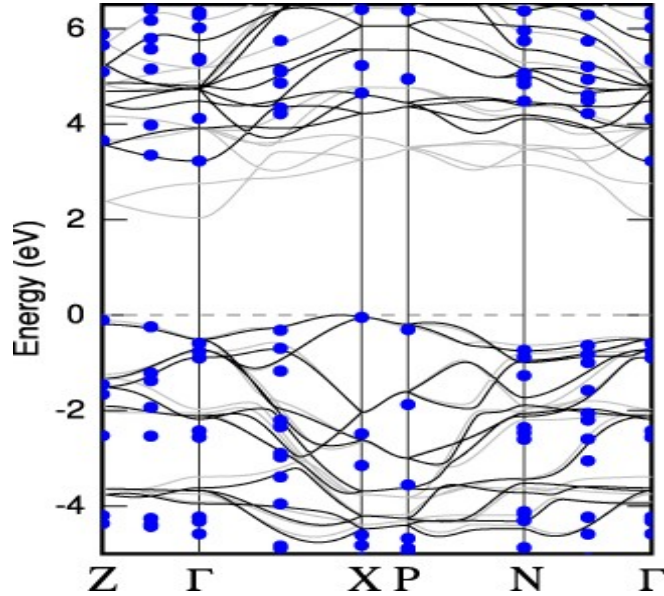
$$H_{cv\mathbf{k},c'v'\mathbf{k}}^{BSE} = H_0 + 2\bar{V} - W$$

Matrix size =  $N_v \times N_c \times N\text{-kpoints}$

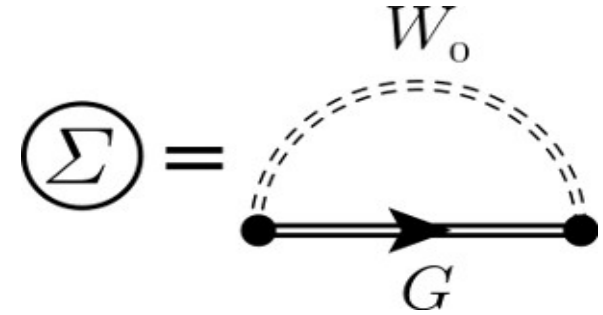
- Small size (Lapack)
- Medium size (Scalpack, Magma, etc..)
- Big size (Haydock + Slepc)



# Quasi-particle band structure 1/2



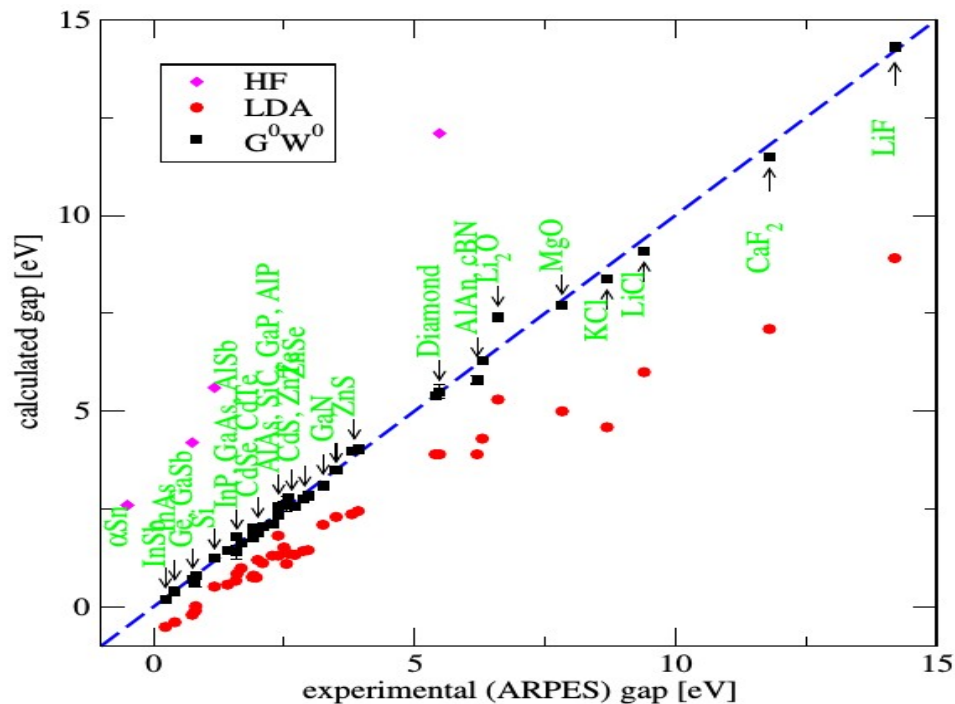
$$W(\omega) = \frac{V}{\epsilon(\omega)}$$



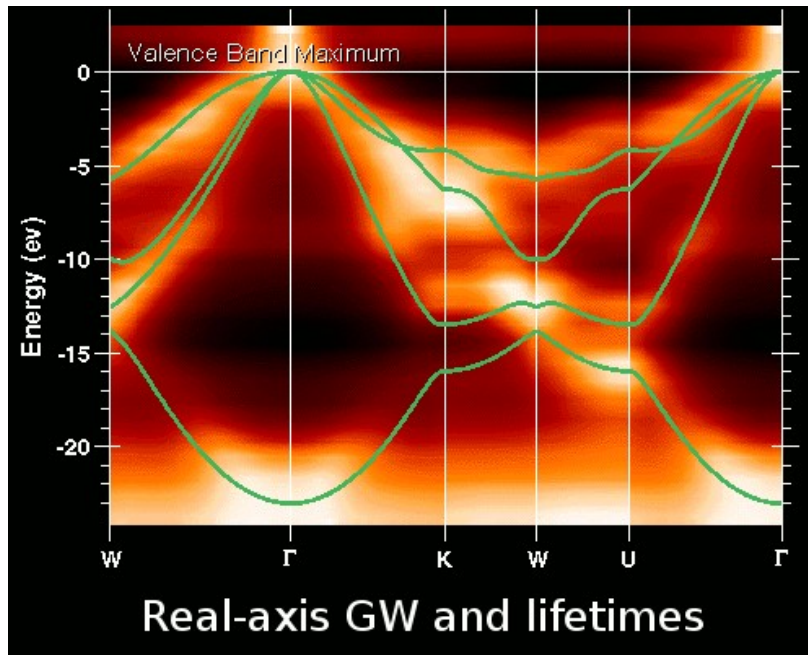
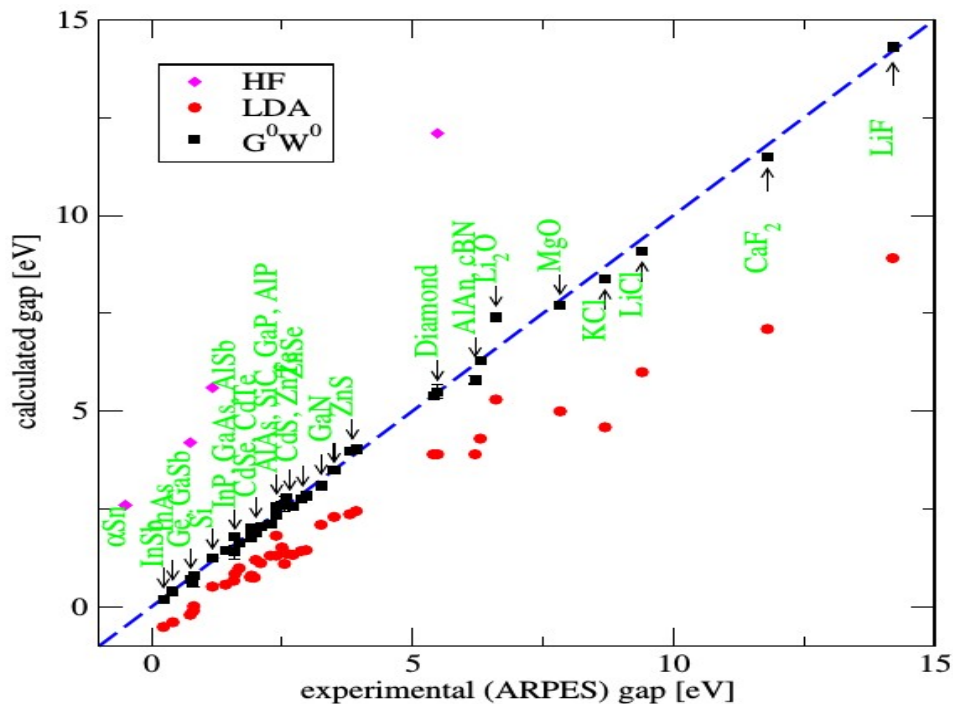
GW is the first order correction in terms of screened interaction

Aryasetiawan, F., & Gunnarsson, O. The GW method. Reports on Progress in Physics, **61**(3), 237.(1998).

# Quasi-particle band structure 2/2



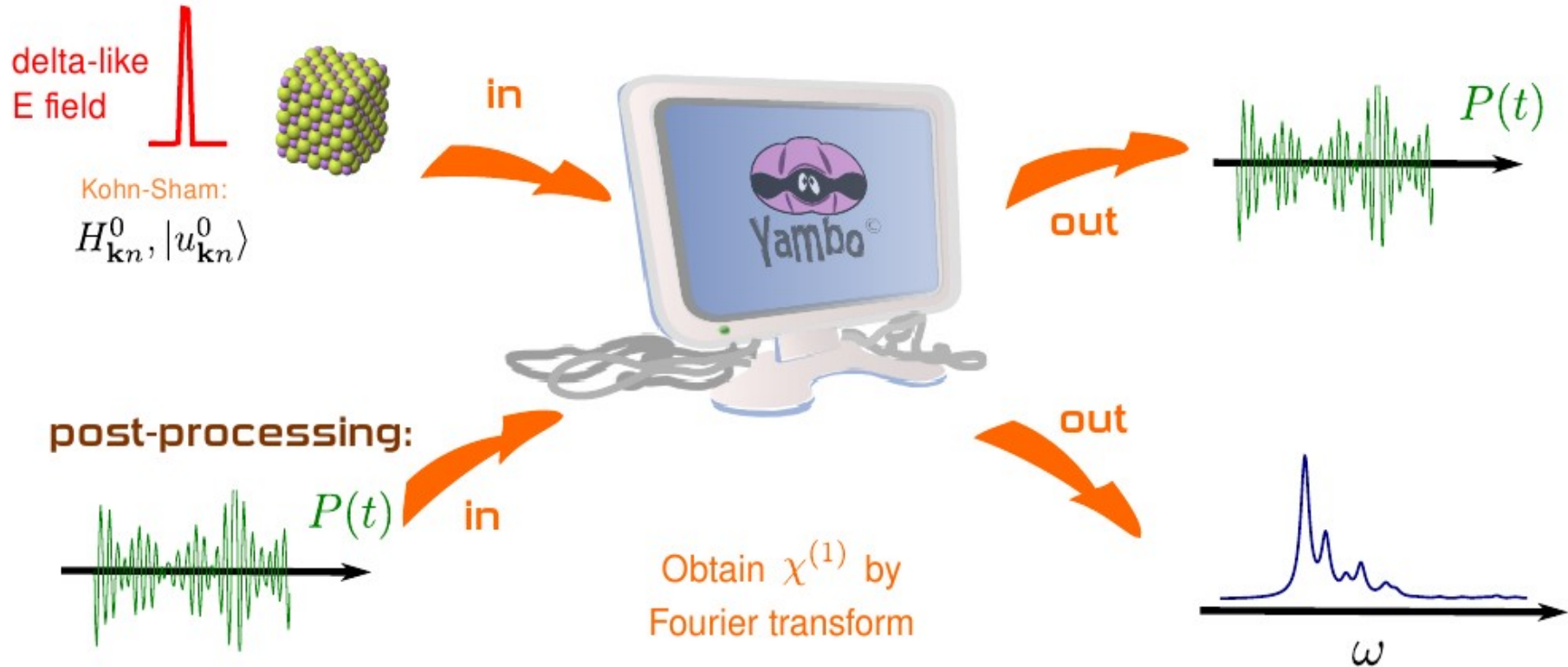
# Quasi-particle band structure 2/2



# Non-linear response

Solve Euler-Lagrange equations:

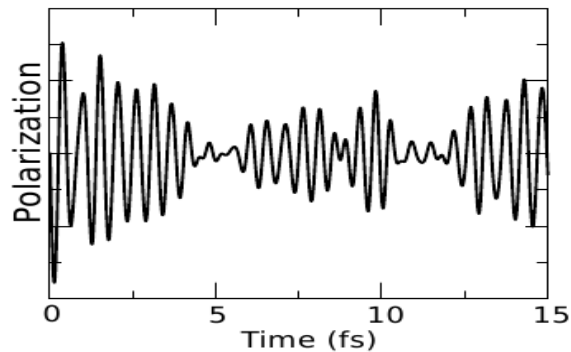
$$i|\dot{v}_{\mathbf{k},m}\rangle = \left( \hat{H}_{\mathbf{k}}^0 + \hat{w}_{\mathbf{k}}(\mathcal{E}) + \hat{w}_{\mathbf{k}}^\dagger(\mathcal{E}) \right) |v_{\mathbf{k},m}\rangle$$



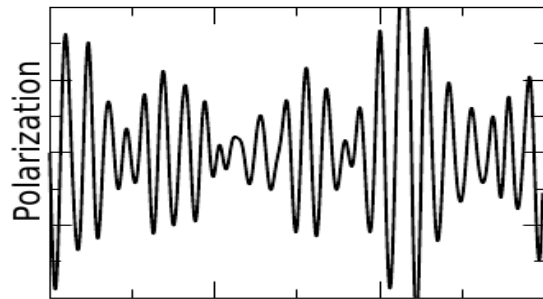
# The Hamiltonian makes the difference

$$H^{eff} = h_k^0 + \Delta h_k + V_H[\Delta \rho] + \Sigma_{sex}[\Delta \gamma]$$

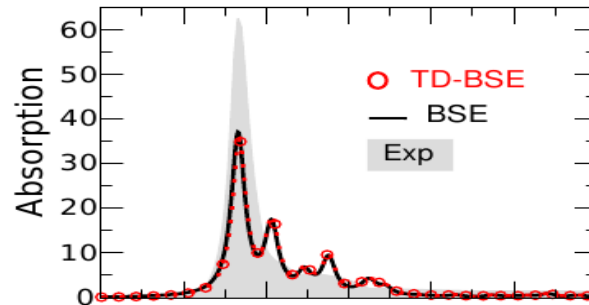
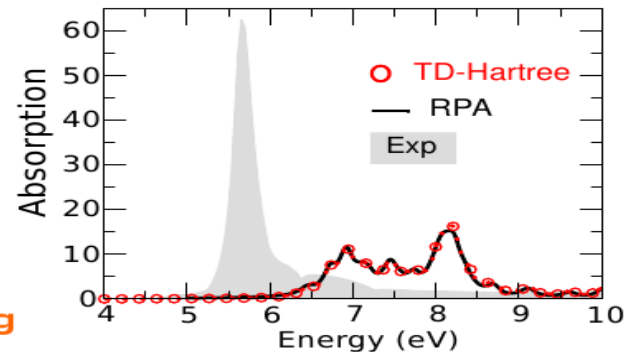
TD-Hartree:



TD-BSE:

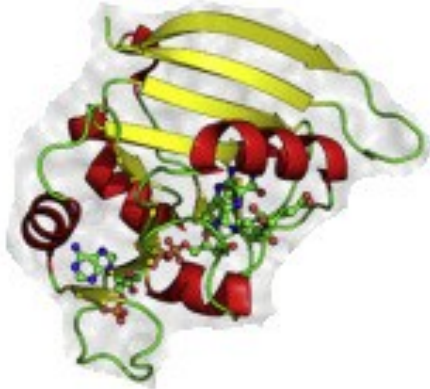


post-processing



# Low dimensional systems

What you would like to  
simulate

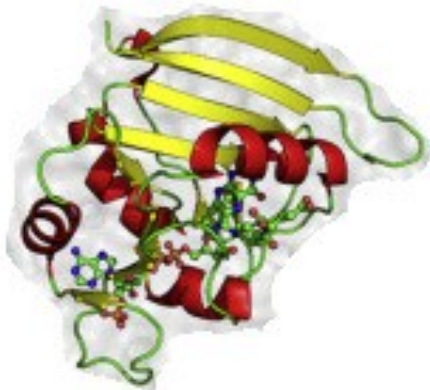


The image is for illustrative purposes only.

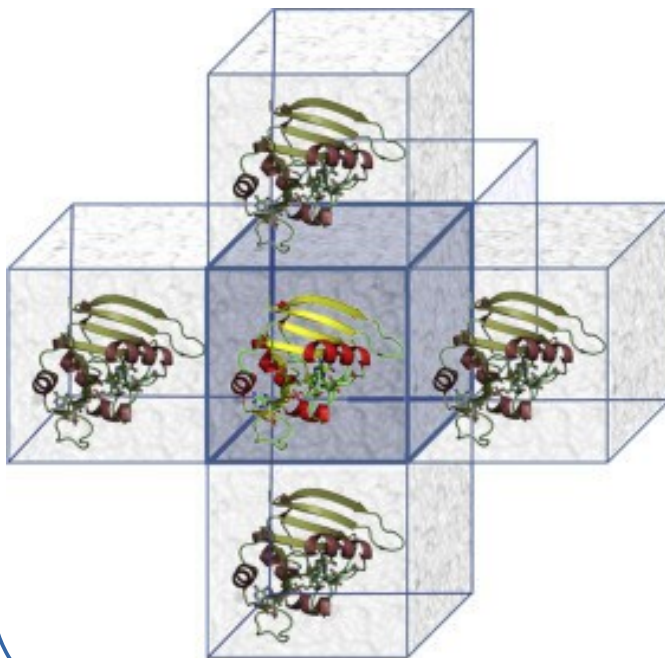


# Low dimensional systems

What you would like to simulate



What you really simulate

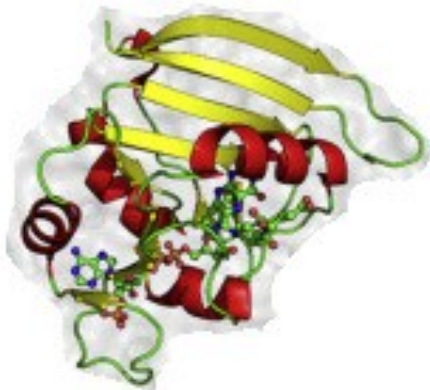


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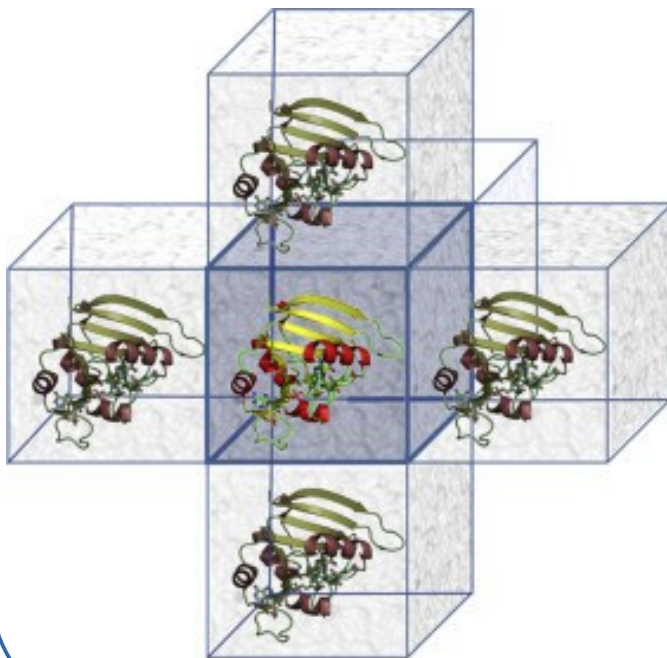


# Low dimensional systems

What you would like to simulate



What you really simulate

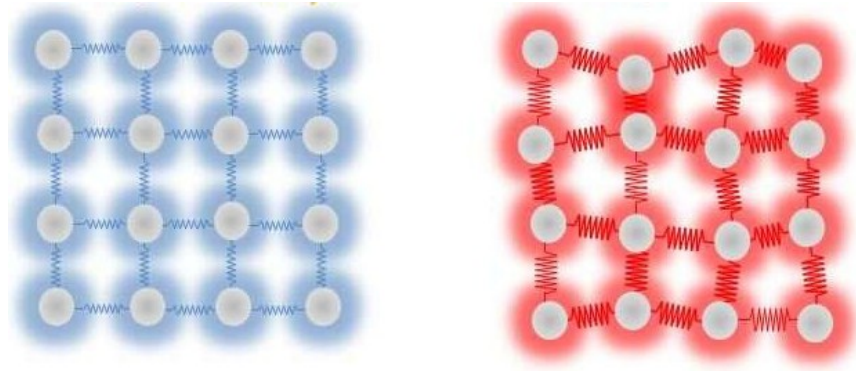


**Solution:**  
**Coulomb cutoff**



The image is for illustrative purposes only.

# Temperature



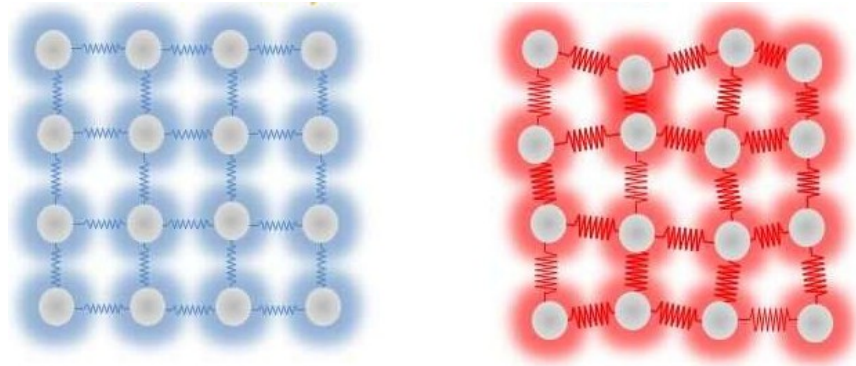
$$\Delta E_{n\mathbf{k}} = \text{SE} + \text{DW}$$

The diagram shows the equation  $\Delta E_{n\mathbf{k}} = \text{SE} + \text{DW}$ . Below the equation, there are two Feynman diagrams. The first diagram, labeled 'SE', consists of a horizontal line with a wavy line (representing a phonon) attached to it. The second diagram, labeled 'DW', consists of a horizontal line with a wavy line (representing a phonon) attached to it, and a small circle with a dot inside (representing a double-well potential) attached to the line.

## Many-Body Effects on the Zero-Point Renormalization of the Band Structure

G. Antonius, S. Ponc , P. Boulanger, M. C t , and X. Gonze  
Phys. Rev. Lett. **112**, 215501 (2014)

# Temperature 1/2

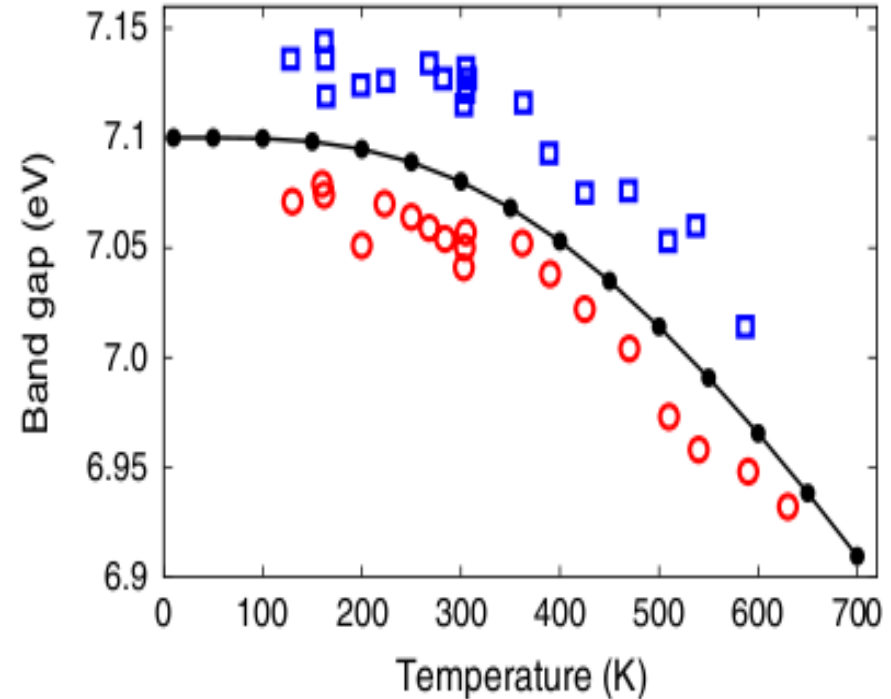


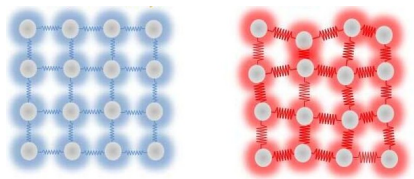
$$\Delta E_{n\mathbf{k}} = \text{SE} + \text{DW}$$

SE                      DW

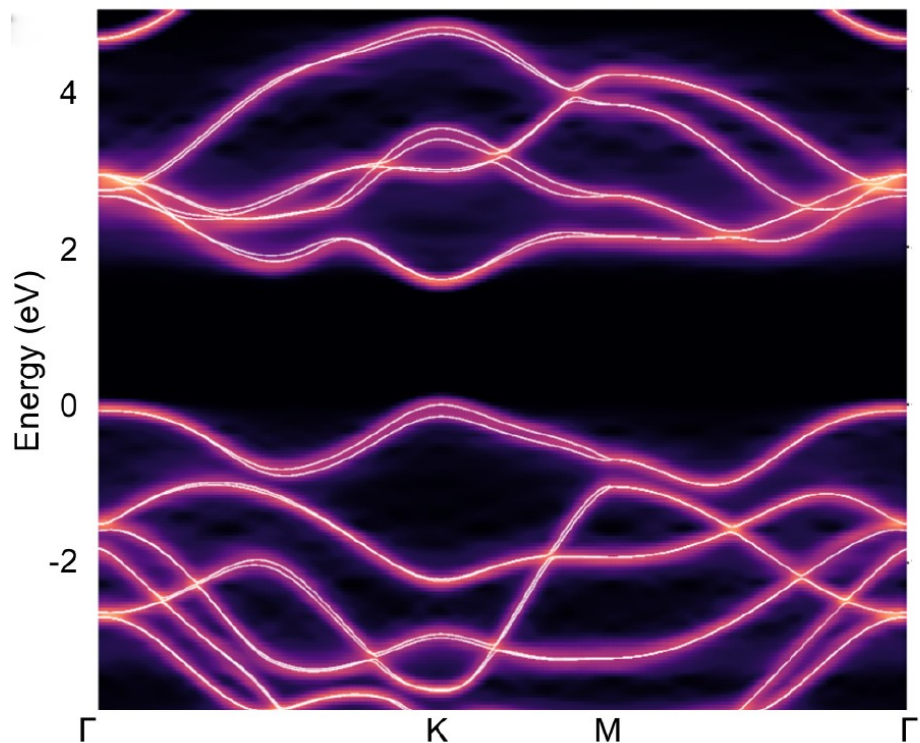
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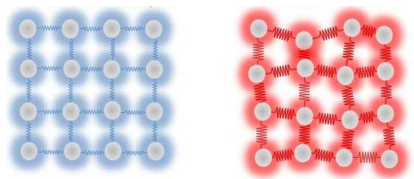


# Temperature 2/2

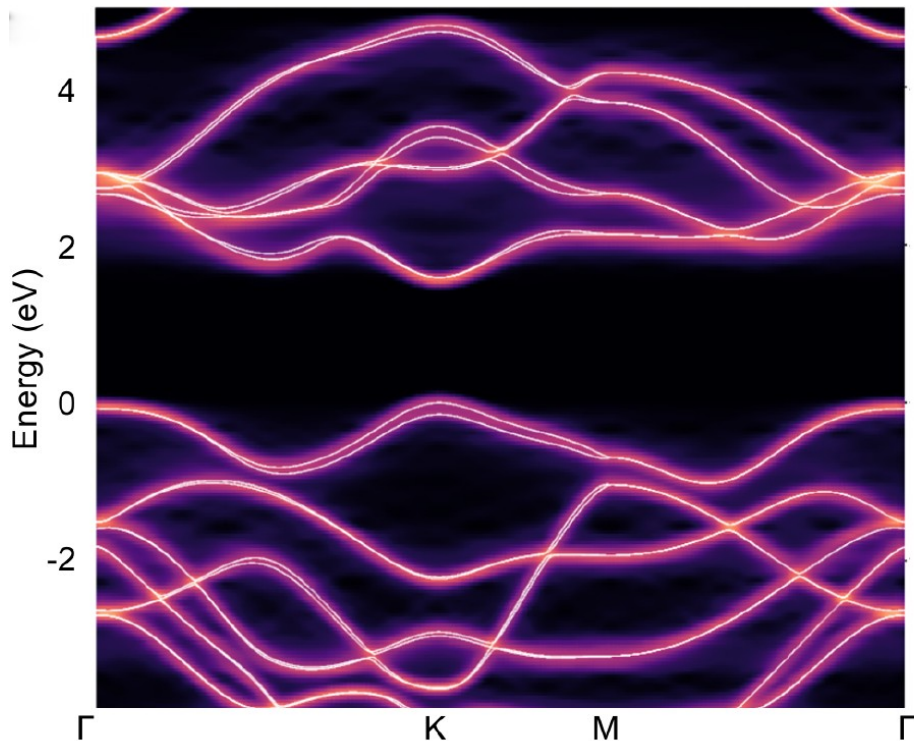


M. Zacharias, F. Giustino, [Phys. Rev. Res. 2, 013357 \(2020\)](#)

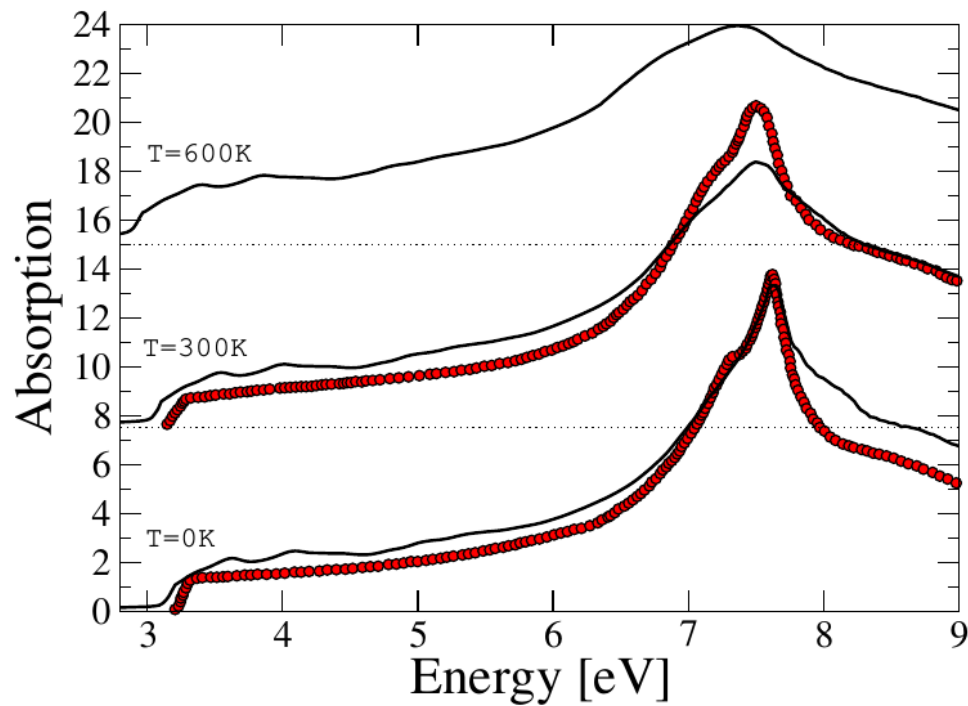




# Temperature 2/2



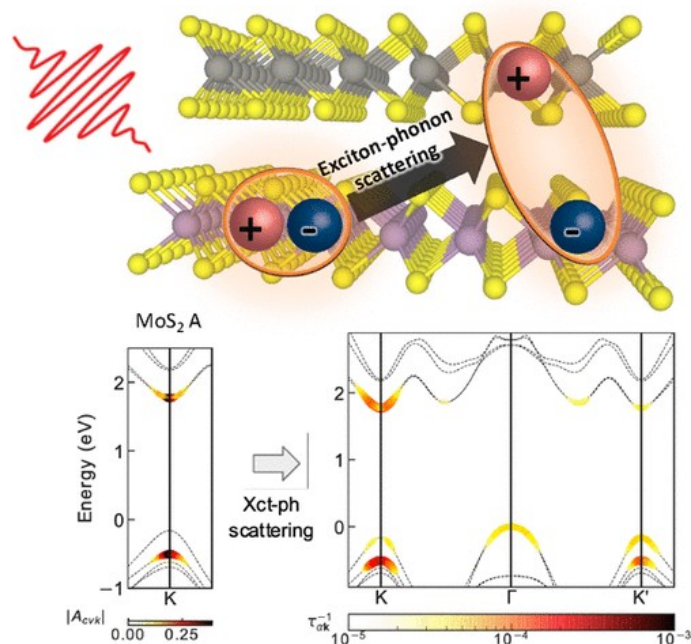
M. Zacharias, F. Giustino, [Phys. Rev. Res. 2, 013357 \(2020\)](#)



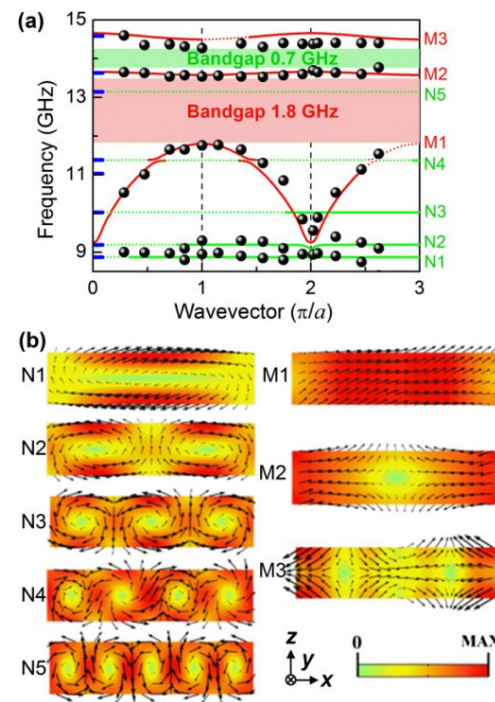
H Kawai, K Yamashita, E Cannuccia, A Marini  
Physical Review B **89** (8), 085202 (2014)



## Exciton-phonon (see Fulvio P. talk)



## Magnons (Alejandro M. S. et al.)



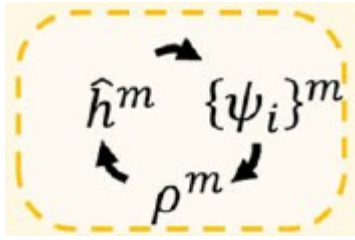


# Typical Yambo calculation



# Yambo calculation in 5 steps

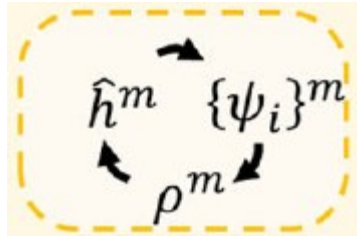
Self-consistent DFT





# Yambo calculation in 5 steps

Self-consistent DFT

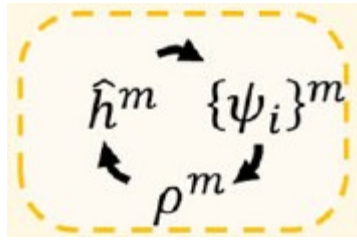


Non-Self-consistent

$$H_{\mathbf{k}}^{KS} |\phi_{n\mathbf{k}}\rangle = \epsilon_{n\mathbf{k}} |\phi_{n\mathbf{k}}\rangle$$

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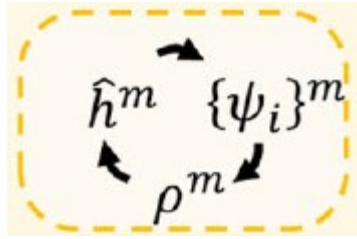


Import in Yambo

*p2y, a2y.....*

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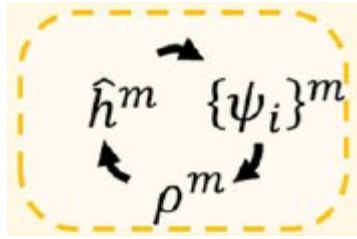
Yambo setup

*./yambo*

↓  
r\_setup

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Self-consistent DFT



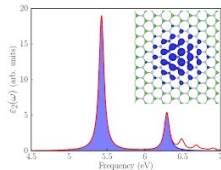
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Import in Yambo

*p2y, a2y.....*

You can run you  
calculation



Yambo setup

*./yambo*

*r\_setup*

# Input and command line

```
$ yambo -h
'A shiny pot of fun and happiness [C.D.Hogan]'
```

This is : yambo  
Version : 5.3.0 Revision 23927 Hash 1730222ea  
Configuration: MPI+OpenMP+SLK+SLEPC+HDF5\_MPI\_IO

...

Initializations:

-setup	(-i)	:Initialization
-coulomb	(-r)	:Coulomb potential
-rw	(-w)	:Screened coulomb potential

Response Functions:

-optics	(-o) <string>	:Linear Response optical properties (more with -h optics)
-X	(-d) <string>	:Inverse Dielectric Matrix (more with -h X)
-dipoles	(-q)	:Oscillator strenghts (or dipoles)
-kernel	(-k) <string>	:Kernel (more with -h kernel)

Self-Energy:

-hf	(-x)	:Hartree-Fock
-gw0	(-p) <string>	:GW approximation (more with -h gw0)
-dyson	(-g) <string>	:Dyson Equation solver (more with -h dyson)
-lifetimes	(-l)	:GoWo Quasiparticle lifetimes

Bethe-Salpeter Equation:

-Ksolver	(-y) <string>	:BSE solver (more with -h Ksolver)
----------	---------------	------------------------------------

Total Energy:

-acfdt		:ACFDT Total Energy
--------	--	---------------------

Utilites:

...

-slktest		:ScaLapack test
----------	--	-----------------

[https://wiki.yambo-code.eu/wiki/index.php?title=First\\_steps:\\_walk\\_through\\_from\\_DFT\(standalone\)](https://wiki.yambo-code.eu/wiki/index.php?title=First_steps:_walk_through_from_DFT(standalone))

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----------	---------------	------------------------------------

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## Utilites:

...

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## Linear optics (IP) - Input generation

```
yambo -F yambo.in_IP -o c
```

## Linear optics (IP) - Run calculation

```
yambo -F yambo.in_IP
```

# Input and command line

## Linear optics (IP) - Input generation

```
yambo -F yambo.in_IP -o c
```

```
optics                # [R] Linear Response optical properties
chi                   # [R][CHI] Dyson equation for Chi.
% QpntsRXd
  1 | 1 |              # [Xd] Transferred momenta
%
% BndsRnXd
  1 | 10 |             # [Xd] Polarization function bands
%
% EnRngeXd
  7.50000 | 25.00000 | eV # [Xd] Energy range
%
% DmRngeXd
  0.100000 | 0.100000 | eV # [Xd] Damping range
%
ETStpsXd= 300         # [Xd] Total Energy steps
% LongDrXd
  1.000000 | 0.000000 | 0.000000 | # [Xd] [cc] Electric Field
%
```

## Linear optics (IP) - Run calculation

```
yambo -F yambo.in_IP
```

# What you really calculate?

(1) Linear response (IP/RPA-NLF): `yambo -optics c`

$$\epsilon_{\alpha,\alpha}(\omega) = 1 + \frac{16\pi}{\Omega} \sum_{c,v} \sum_{\mathbf{k}} \frac{1}{E_{c\mathbf{k}} - E_{v\mathbf{k}}} \frac{|\langle v\mathbf{k} | \mathbf{p}_{\alpha} + i[V^{\text{NL}}, \mathbf{r}_{\alpha}] | c\mathbf{k} \rangle|^2}{(E_{c\mathbf{k}} - E_{v\mathbf{k}})^2 - (\omega + i\gamma)^2}$$

See (2)

```
% LongDrXd
1.000 | 0.000 | 0.000 |
%
```

**E-field direction (for q=0)**  
Vector (cartesian coordinate)  
Refers to first q-point (`QpntsRXd`)

DFT  
k-grid

```
% EnRngeXd
0.000 | 10.000 | eV
%
```

**ETStepsXd = 100**  
**Energy grid in output**  
Range from 0 to 10 in 100 steps

```
% BndsRnXd
1 | 100 |
```

**Bands used (empty & filled)**  
Range from 1 to nbnd  
Reduce range to lower memory. In metals, includes partially filled bands. See also `EhEngyXd (-V all)`

```
% DmRngeXd
0.1000 | 0.100 | eV
%
```

**Broadening of spectra**  
Either a fixed value, or linearly changing between 2 values



# Input and command line

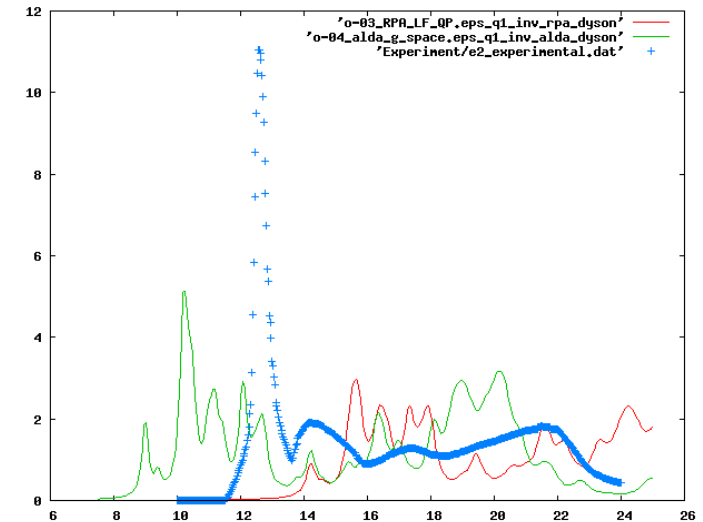
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## Linear optics (IP) - Run calculation

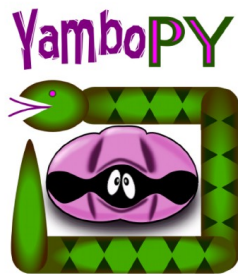
```
yambo -F yambo.in_IP
```



LiF

# Post-processing



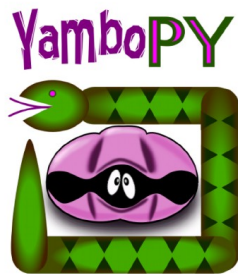


# YamboPy 1/4

## Yambopy goals:

- QE and Yambo interface
- Access binary databases
- Scripting
- Pre/Postprocessing
- Plotting
- Workflows
- Aida plugin
- Utilities
- Quality-of-life tweaks
- *Open to user tinkering*





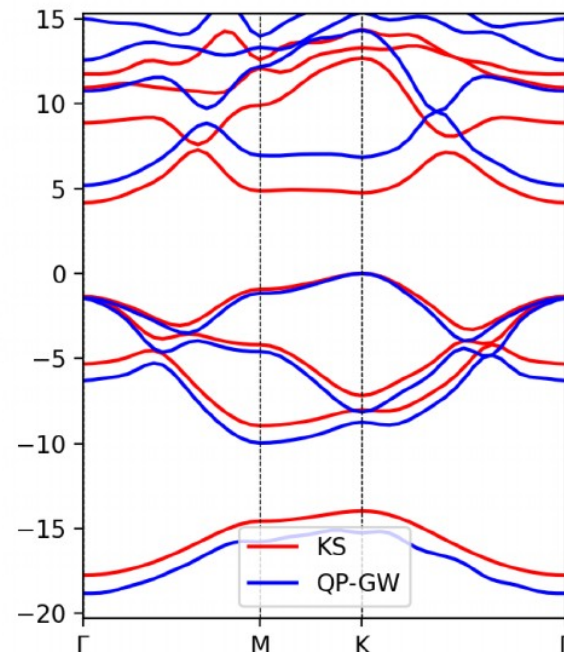
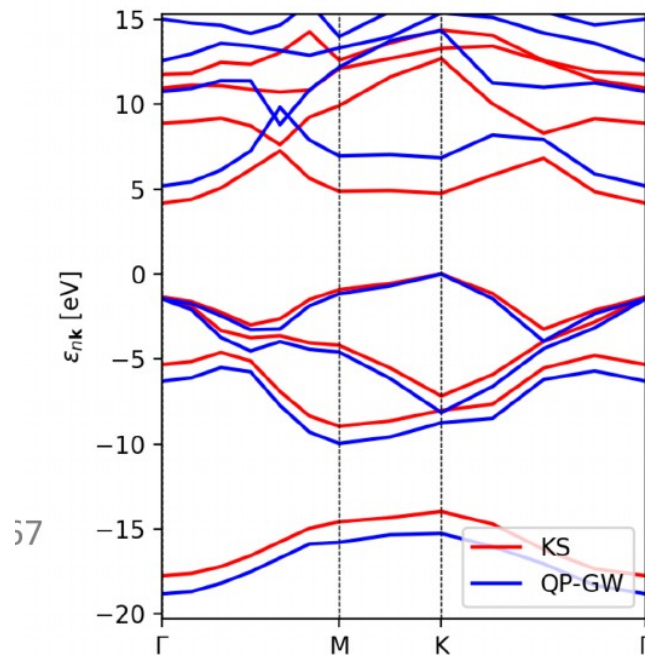
# YamboPy 1/4

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Smooth Fourier interpolation  
(SKW method) imported from

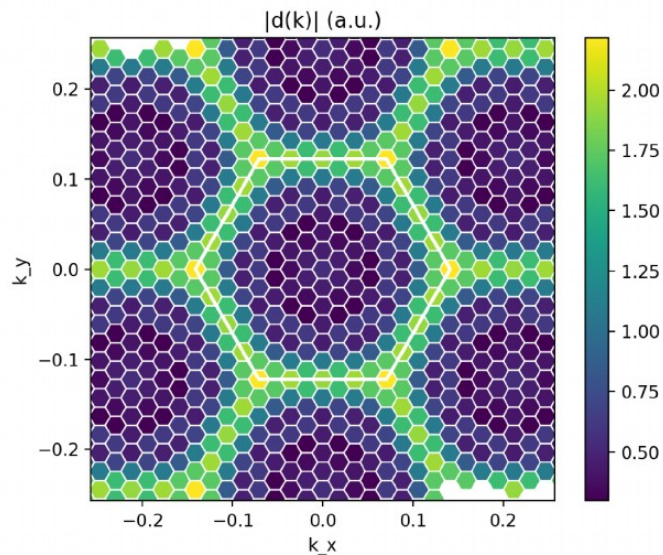




# YamboPy 2/4: visualization

```
from yambopy import YamboDipolesDB
```

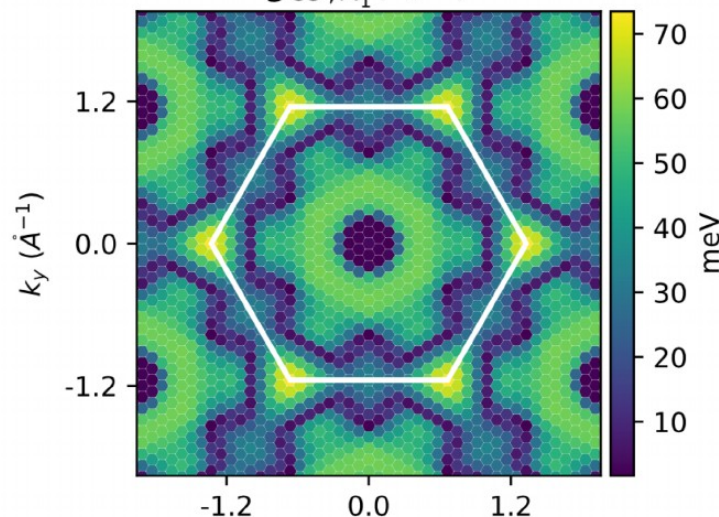
$$d_{cvk} = \langle ck | \epsilon \cdot \hat{\mathbf{r}} | vk \rangle$$



```
from yambopy import YamboElectronPhononDB
```

$$g_{cvk}^{\mu}(\mathbf{k}, \mathbf{q}) = \frac{1}{\sqrt{2\Omega_{q\mu}}} \langle ck | \partial_{q\mu} V_{\text{SCF}}(\mathbf{q}) | vk - q \rangle$$

$$< g_{cc', A'_1}(\Gamma; \mathbf{k}) >$$



Monolayer MoS2

# YamboPy 3/4: exciton analysis

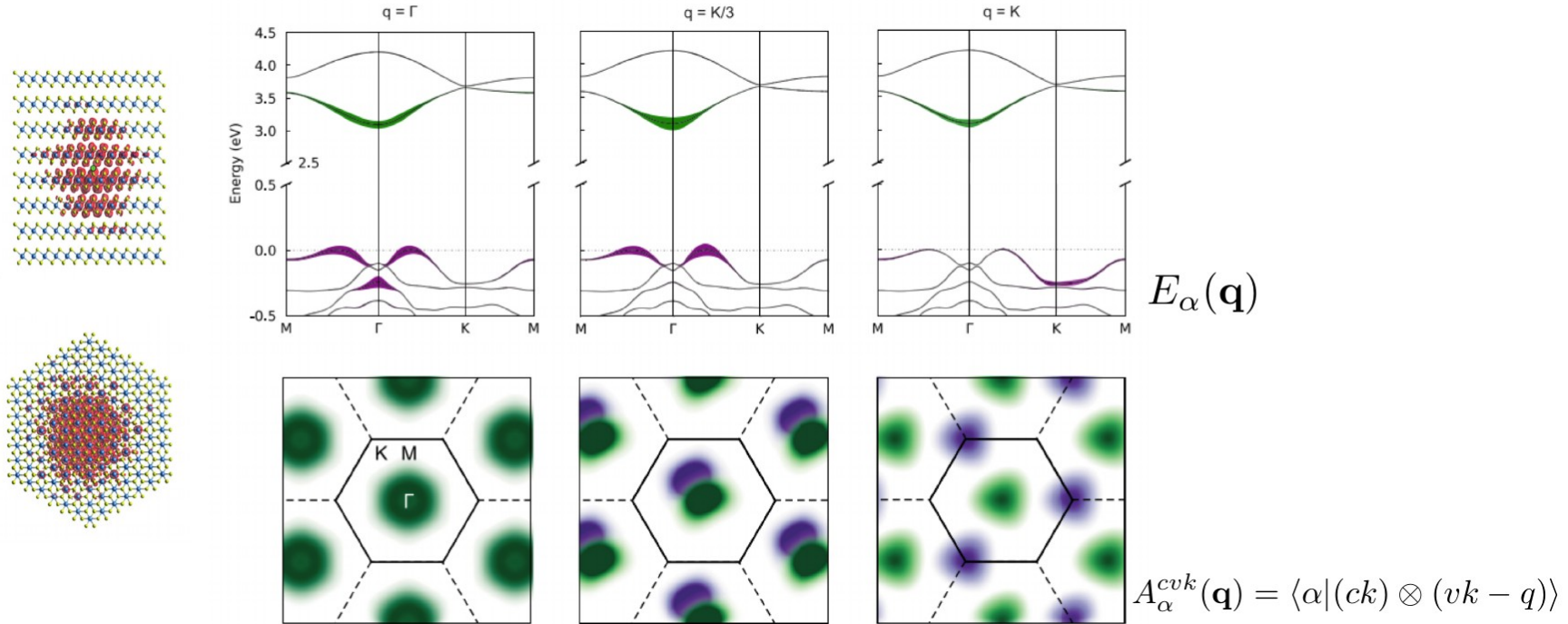
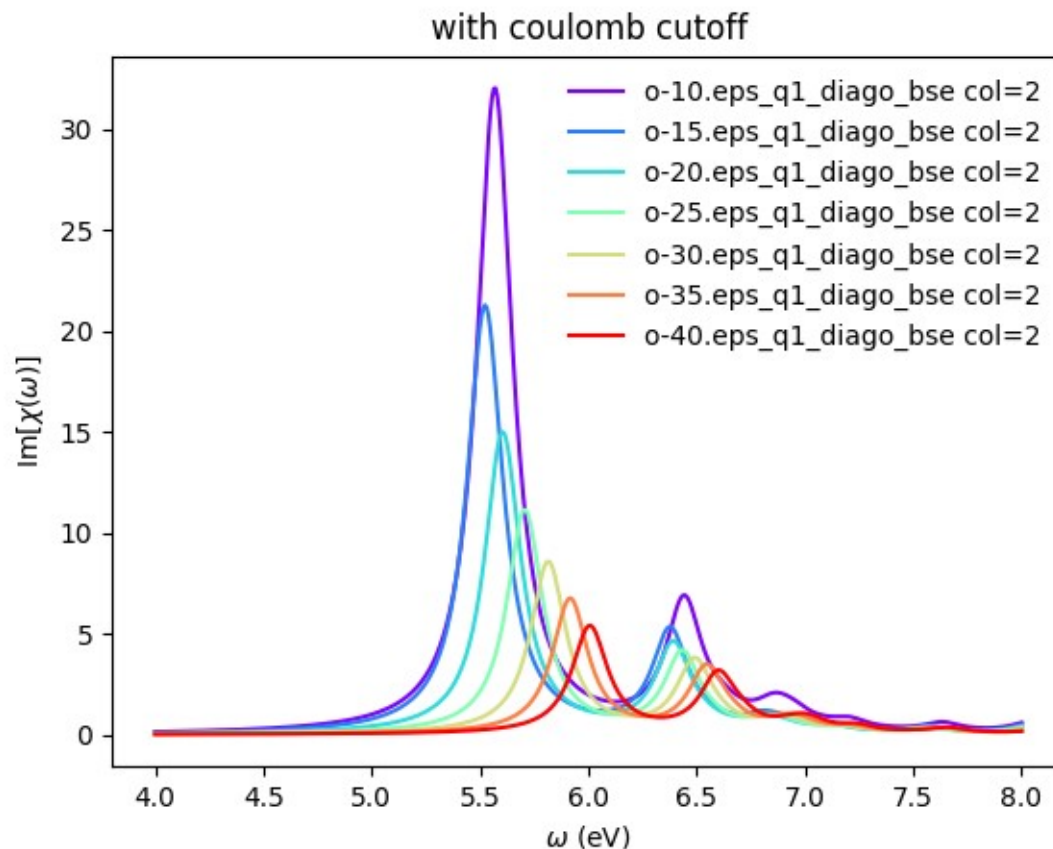
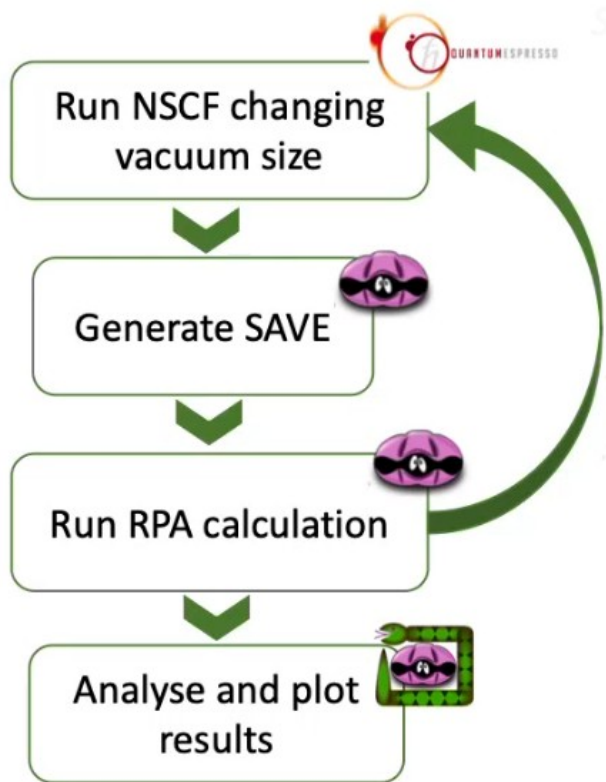


Figure on bulk BiI<sub>3</sub> by Jorge Cervantes-Villanueva.  
PRB **109** 155133 (2024)

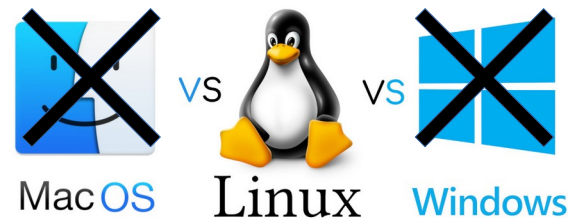
# YamboPy 4/4: workflow



<https://www.youtube.com/watch?v=gStCeigSXS0>



# Installation



## Required libraries (included in Yambo)

- Lapack/Blas
- NetCDF (to be removed soon)
- HDF5

## Optional libraries

- Scalapack
- Slepch/Petsc
- Yaml/Magma etc....

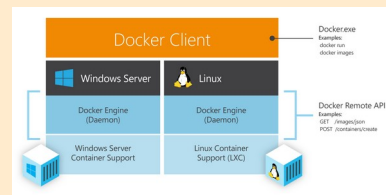
## Installation instructions



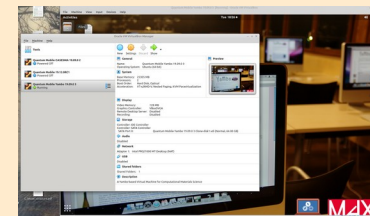
- Linux Ubuntu/LinuxMint (gfortran| intel | nvdia)
- MacOSX (ARM)
- Machine specific (Leonardo, Irene,...)

## Virtual Machines

### Docker



### VirtualBox



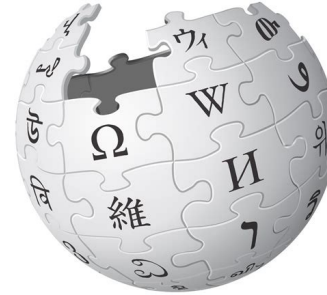




# Thank you for your attention



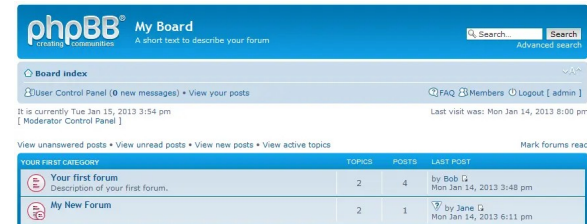
<https://www.yambo-code.eu/>



[https://wiki.yambo-code.eu/wiki/index.php/Main\\_Page](https://wiki.yambo-code.eu/wiki/index.php/Main_Page)



<https://www.youtube.com/@yambocode2721>



<https://www.yambo-code.eu/forum/>